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Calculation of Collision Speed Corresponded to Maximum Penetration Using Hydrodynamic Theory

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ABSTRACT

One of the most valid and efficient models of long rod projectile penetration in homogeneous targets is Tate and Alekseevskii's (A&t) model. Based on Tate's model, the present paper tries to calculate the optimum speeds to achieve the maximum penetration depth in the homogeneous targets. The proposed collision speed-penetration depth diagrams are developed using Tate's model. In this way, various collision speed-penetration depth diagrams for different projectile dynamic resistances and targets are calculated and the optimum speed envelope is derived. According to Tate's diagrams, the increase of collision speed is not followed by the increase of penetration depth; instead, it causes erosion phenomenon to happen. The comparison of the resulted optimum penetration speeds and the available data confirms the findings. Speed and rigidity both have a positive impact on the increase of penetration depth. With the increase of speed, the erosion issue finds a higher significance due to the increase of pressure on the projectile tip. Therefore, higher speed and erosion are opposed to each other; for the case of Y>R, there are some maximum points which indicate the optimum reciprocity of the two mentioned factors to obtain a maximum penetration depth. In the present paper, an equation is developed indicating the optimum speeds resulting in the maximum penetration rate in the case of Y>R. For the reciprocity of speed and erosion, the target resistance against an erosive projectile should be 4 to 5 fold higher than the same target resistance against a rigid projectile penetration. [4]

KEYWORDS: hydrodynamic theory; Tate and Alekseevskii's theory; erosion; rigidity; optimum speed; maximum penetration depth.

IINTRODUCTION

When a projectile penetrates into a semi-infinite concrete target, it continuously pushes the target materials and drives it toward a radius of its front section [1-3]. If the pressure applied on the contact point between the projectile tip and the target is higher than the projectile resistance, its tip deformation will happen and it changes to a mushroom-like shape (mushrooming phenomenon). This deformation varies depending on collision speed as well as projectile and target relative resistances. For collision speeds lower than 1000m/s, there is no significant deformation in the projectile [1], so in this case the hypothesized undeformability of projectile tip will be met. In such a case, there is a linear relation between the penetration depth and collision speed [2] which is calculated using the expansion theory for concrete target resistance cavity against the movement of rigid projectile and ultimately, the penetration depth is calculated.

MATERIALS AND METHODS

With the increase of collision speed, the erosion phenomenon begins at the projectile, its tip changes to mushroom form and its materials are ejected into the surrounding environment. It causes some wasting in energy along with an outstanding efficiency reduction of projectile penetration into the target. Unfortunately, there is a lack of experimental data about the penetration into the concrete targets at 1000m/s or more speeds. The extant data for tungsten and tantalum projectiles relates to 3900m/s to 4600m/s collision speeds [5]. The penetration depth into concrete target is proportional to reduction in the length of projectile rode indicating an agreement with the penetration hydrodynamic theory. Using reverse ballistic experiments, Miler and Mckay tried to study the penetration of tungsten projectiles at 900m/s to 4300m/s speeds. Although there is a dispersed data in this respect, it shows an acceptable agreement with hydrodynamic theory. The present relatively scant data for collision speeds lower than 2000m/s indicates the reduction of cavity diameter in the target (decrease of mushrooming phenomenon).

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The fact reveals the possibility of intermediate cases and expression of the projectile and target resistances impacts. What is studied and tested in the present paper relates to collision speeds higher than 1200 m/s to 1600 m/s. In such speeds, the projectile and target resistances are manifested and so should be considered in the equations. It is thus inevitable to use the penetration equations developed by Tate and Alekseevskii instead of hydrodynamic theory.

DISCUSSION

The above mentioned facts lead us to use the erosive penetration model for long rod projectiles in the semiinfinite concrete target considering resistance impacts of projectile and target. The solution of the following equation is used to obtain a closed solution for *l*:

The solution of the following equation is used to obtain a closed solution for l:

$$\frac{dl}{l} = \frac{\rho_p (v - \frac{v - \mu (v^2 + A)^{\overline{2}}}{1 - \mu^2})}{Y_p} dv \Longrightarrow l(v, v_0)$$

Based on the relation, l is derived according to $v_{and}v_0$. For $R_t < Y_p$, the penetration depth is obtained from the following integral.

$$P = \frac{\rho_p}{Y_p} \int_{v_0}^{v_{cr}} u l dv = \frac{\rho_p}{Y_p} \int_{v_0}^{v_{cr}} \frac{v - \mu(v^2 + A)^{\frac{1}{2}}}{1 - \mu^2} l(v, v0) dv$$

$$A = \frac{2(R_t - Y_p)(1 - \mu^2)}{\rho_t}$$

Since p_t , so the above relation is considered as a function of following variables: $\frac{P}{L} = F(v_0, \rho_p, \rho_t, R_t, Y_p)$

It means that for constant ρ_p , ρ_t and R_t , it is possible to obtain corresponding values for each Y_p in lieu of variable v_0 . For instance, for $\rho_p = \rho_t = 7850$ and $R_t = 50MPa$ with $v_0 > v_{cr}$, the following figure is obtained (in which Yp=variable, Rt=cte, vertical axis shows p/l ratio and horizontal axis indicates v_0 value).



As it can be seen from the figure, $Y_p = 1.1E9$ changes to $Y_p = 9.1E9$. Toward the right side of the figure, diagrams show the increase of Y_p .

It is possible to draw the diagram with a changing R_t and a constant Y_p . For example, for a constant $\rho_p = \rho_t = 7850$ and $Y_p = 500MPa$ with changing R_t , the following figure is obtained for each changing v_0 's (in which Rt=variable, Yp =cte, vertical axis shows p/l ratio and horizontal axis indicates v_0 values).



As it can be seen in the figure, $R_t = 0.5E8$ changes to $R_t = 4.5E8$. In the bottom of the figure, diagrams show the increase of R_t . Here, the main purpose is to drive a relation for each specific ρ_p , ρ_t and to calculate v_0 value according to the maximum penetration depth which for simplicity is called v_m and also to determine its corresponding maximum penetration value, P_m . The above figures show that effectiveness of changing in Y_p on v_m is more than R_t .

The important point here is that with regard to the extant relations, the maximum is achieved only with $R_t < Y_p$. Using Lybernitz relation, differentiation of penetration depth integral gives:

$$P = \int_{v_0}^{v_{cr}} G(v, v_0) dv \Longrightarrow \frac{\partial P}{\partial v_0} = \int_{v_0}^{v_{cr}} \frac{\partial G}{\partial v_0} dv - L = 0$$

In this way, the above equation is solved as an integral equation. Based on the complex formulation of function G, it is not possible to calculate the integral as usual (except under specific conditions). Therefore, the integral is drawn using numerical method for different R_t and Y_p values. In the following figure, the maximum values of R_t and Y_p are connected through straight lines.

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As it can be observed, the maximum values are not positioned in a straight line. The figure is drawn for different R_t and Y_p values and similar to the above procedure, the maximum values are connected through straight lines. For more simplicity, only maximum values are marked. It is worth mentioning that $\rho_p = \rho_t = 7850$ are selected for the following figures.



Regarding the marked points, different curves were tested for fitting purposes and finally a curve with the below pattern was selected as the curve with highest goodness of fit and lowest error. It is necessary to mention that individual relations are proposed:

$$x_1 = Ln(R_t) \quad ; \quad x_2 = Ln(Y_p)$$

$$Ln(v_m) = a_0 + a_1x_1 + a_2x_2 + a_3x_1^2 + a_4x_2^2 + a_5x_1x_2$$

$$(P/L)_m = a_0 + a_1x_1 + a_2x_2 + a_3x_1^2 + a_4x_2^2 + a_5x_1x_2$$

Coefficients for each term are given in the following table:

	0.7506	0.1146	0.0020	0.0048	0.0142	-0.0106
$(P/L)_m$	1.2779	-0.8038	0.7723	0.0076	0.0105	-0.0179

In the following figure, the resulted curve obtained from the above fitted curve is shown comparing v_m primary data. The error rate resulted from the above examination of fit goodness is 0.8764 percent (vertical axis shows v_m ration and horizontal axis indicates $(P/L)_m$ values).



The following figure also reveals the resulted curve obtained from the above fitted curve for $(P/L)_m$ primary data (vertical axis shows V_m ration and horizontal axis indicates $(P/L)_m$ values)



For example, assume $R_t = 200MPa$ and $Y_p = 500Mpa$.

Thus:

$$x_1 = Ln(R_t) = 19.1138$$
; $x_2 = Ln(Y_p) = 20.0301$

Using the first row in the above mentioned table:

$$Ln(v_m) = a_0 + a_1 x_1 + a_2 x_2 + a_3 x_1^2 + a_4 x_2^2 + a_5 x_1 x_2 = 6.3774 \Longrightarrow v_m = 588.3676$$

and according to the second row in the table, we have:

$$(P/L)_m = a_0 + a_1 x_1 + a_2 x_2 + a_3 x_1^2 + a_4 x_2^2 + a_5 x_1 x_2 = 1.5231$$

RESULTS

When there are extreme points in the Tate graphs and R is greater than that of Y, the projectile is rigid enough. Therefore, proportional to the projectile rigidity, optimized velocity has a lot to shoot with the speed and will cause optimal performance of the projectile and will get the maximal depth. In This paper, curve fit equation obtained from this particular case is not bound trapped. Thus, it can be used for designing the resistance of the target projectile in this paper. In addition to gained results, it is acceptable to emphasize the capability of Tate graphs because we managed to do a kind of optimization and estimate the maximal depth and obtain optimized speed as well.

The following figure shows the corresponding diagram. As it can be seen, the empirically obtained values are in agreement with the following diagram:



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